Feed Horn Coupled Bolometer Arrays for SPIRE: Design, Simulations, and Measurements

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Abstract

In this paper, we present the design, modeling, and measurements of antenna coupled large bolometer arrays being developed for the Herschel space observatory’s Spectral and Photometric Imaging REceiver (SPIRE) instrument. SPIRE has five arrays of feed horn coupled silicon nitride micromesh “spider-web” bolometers in two instruments, a three-band photometer and a two-band Fourier transform spectrometer, each covering the 430 GHz – 1.5 THz band. The optical coupling efficiency, bandwidth, and cross-talk between adjacent pixels of the arrays were investigated with numerical electromagnetic field simulators, and prototype arrays were measured extensively in a test facility. The measured results were found to be in good agreement with simulation predictions, and the simulation results were used as a benchmark for the design goals of the instrument.

I. Introduction

One of the pressing questions of modern astrophysics today is how galaxies and stars are formed. It is widely believed that the answer to that lies in the close study of the submillimeter and far infrared (FIR) spectrum of the sky. Our universe is most luminous in this frequency range after the cosmic microwave background radiation. Radiation at these wavelengths where interstellar dust is transparent enables observations of star formation deeply embedded in molecular clouds. The Herschel Space Observatory (formerly known as FIRST) \(^1\) – a European Space Agency (ESA) cornerstone mission scheduled for launch in 2007, covers approximately the 60 µm – 700 µm (5 THz – 430 GHz) range. The Spectral and Photometric Imaging REceiver (SPIRE) \(^2\) is one of the three cryogenic focal plane instruments on board the Herschel Space Observatory. The main scientific objectives of the SPIRE instrument are deep extragalactic and galactic imaging surveys and spectroscopy of star-forming regions in our own and other nearby galaxies.

SPIRE is composed of two complimentary instruments, a three-band imaging photometer and a two-band imaging Fourier Transform Spectrometer (FTS), each covering the 200 µm – 700 µm (1.5 THz – 430 GHz) band. Both instruments use 0.3 Kelvin feed horn coupled silicon nitride (Si\(_3\)N\(_4\)) micromesh “spider-web” bolometers \(^3\) which have been very successful in ground-based and sub-orbital millimeter-wave instruments. The multi-frequency photometer instrument on SPIRE has three simultaneously-imaging bolometer arrays with 139, 88, and 43 bolometers, in bands centered at 250 µm, 363 µm, and 517 µm wavelengths respectively. The spectral resolution (\(\lambda/\Delta\lambda\)) of the broadband photometer is expected to be around 3. The FTS instrument has two simultaneously imaging arrays of 37 and 19
bolometers, covering 200 $\mu$m – 325 $\mu$m and 306 $\mu$m – 670 $\mu$m wavelengths respectively. The FTS will be operated in continuous scan mode with adjustable optical path length, giving spectral resolution in the range of 1000 – 20 at 250 $\mu$m wavelength. The photometer and the FTS are not designed to operate simultaneously.

The design and development of large arrays of feed horn coupled bolometers at sub-millimeter wavelengths has come a long way. This is primarily due to the tremendous improvement in electromagnetic simulation capabilities over the last couple of years and recent advances in micromesh bolometer fabrication techniques, allowing high yield absorber arrays with bolometer detectors on individual silicon wafers. All these advancements were used in designing the SPIRE instrument. The photometers and the FTSs in SPIRE are packed hexagonally on planar wafers sandwiched between a planar backshort plate and precision feed horn block. The feed horns are terminated in circular waveguides followed by integrating cavities formed by the backshort plate, the silicon substrate wafer, and the feed horn block. The monolithic design of the micromesh absorber and the backshort wafer allows efficient packing of these arrays in a simple fixture.

II. Design and Simulations

A schematic of the SPIRE detector array, showing the details of a single pixel, is shown in Fig. 1. Each pixel has a conical feed horn connected to a circular waveguide. The horns for the array are constructed as a single piece by electroforming – electro-plating copper on carbide-turned aluminum mandrels. To minimize heat capacity and cross-section to cosmic ray absorption, the bolometer absorbers have a “spider-web” architecture. The detector wafer has 1.8 $\mu$m thick Si$_3$N$_4$ micromesh absorber patterned on a 350 $\mu$m thick silicon wafer has 1 carbide-turned aluminum mandrels. To minimize heat capacity and cross-section to cosmic
Neutron-transmutation-doped (NTD) germanium (Ge) thermistors are indium bump bonded to the absorbers. The detector wafer is mounted on a second metalized silicon wafer which has been etched to form tuned backshorts. The detector wafer and the backshort wafer combination is fixed to an invar backplate. Invar is used to minimize mechanical stress on silicon during thermal recycling, and to keep the detectors aligned. The feed horn block is mounted on the invar backplate so that it is suspended over the detector wafer and maintains a safe vacuum gap between them. The lower half of the feed horn block, referred as the “frontshort”, and the backshort along with the detector form the integrating cavity. The cavities are circularly symmetric about the axis of the circular waveguides connected to the feed horns. The integrating cavity has a diameter of 6.5\(\lambda_0\), with 4.5\(\lambda_0\) diameter micromesh absorber sitting at about \(\lambda_0/4\) distance from both the frontshort and the backshort for optimum absorption. \(\lambda_0\) is the free-space wavelength at the band center of the different photometers and the FTSs. It can be seen from Fig. 1 that there is a \(\lambda_0/4\) vacuum gap in each pixel which will allow cavity energy to leak from one pixel to the other, possibly degrading isolation between adjacent cavities. For convenience, the five SPIRE detector arrays have been designated “P/SW”, “P/MW”, and “P/LW” for the short, medium, and long wavelength photometers, and “S/SW” and “S/LW” for the short and long wavelength spectrometers, respectively. For each array, the dimensions indicated in Fig. 1 are listed in Table I.

### A. Simulation Setup

The basic objective of our simulations was to design, optimize, and predict performance of the bolometric integrating cavities. We used Ansoft’s high frequency structure simulator (HFSS) [4] for simulating SPIRE’s integrating cavities. HFSS solves electromagnetic field parameters in arbitrary three dimensional structures using finite-element techniques. HFSS is ideal for our simulations because the calculated field quantities inside the cavities can be accessed, thereby allowing the optical coupling efficiency to be estimated. HFSS has been used before for integrating cavity coupling efficiency calculations by using a simple technique where the differences in the S-parameters, with and without the absorber inside the cavity, were used for predicting reflected and absorbed power in the cavity [5], [6]. Due to the tremendous improvement in HFSS capabilities and phenomenal improvement of computer speeds over the last couple of years, it is now possible to carry out more sophis-

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**TABLE I**

**Feed horn and Cavity Dimensions**

<table>
<thead>
<tr>
<th>Array</th>
<th>(\lambda_0) ((\mu m))</th>
<th>Length, L (mm)</th>
<th>Aperture, A (mm)</th>
<th>Waveguide Dia., D ((\mu m))</th>
<th>Waveguide Length, W ((\mu m))</th>
</tr>
</thead>
<tbody>
<tr>
<td>P/SW</td>
<td>250</td>
<td>23.68</td>
<td>2.40</td>
<td>171</td>
<td>500</td>
</tr>
<tr>
<td>P/MW</td>
<td>363</td>
<td>32.75</td>
<td>3.23</td>
<td>239</td>
<td>700</td>
</tr>
<tr>
<td>P/LW</td>
<td>517</td>
<td>46.36</td>
<td>4.90</td>
<td>342</td>
<td>1000</td>
</tr>
<tr>
<td>S/SW</td>
<td>275</td>
<td>23.68</td>
<td>2.15</td>
<td>190</td>
<td>550</td>
</tr>
<tr>
<td>S/LW</td>
<td>450</td>
<td>46.36</td>
<td>3.80</td>
<td>393</td>
<td>900</td>
</tr>
</tbody>
</table>
ticated and detailed simulations, and consequently to perform electromagnetic calculations to optimize and predict performance of large arrays of antenna coupled integrating cavities.

Given that the cavities are larger than a wavelength, it was impossible to simulate an entire array in a single simulation using HFSS. So, we simulated an array of pixels by modeling a single pixel and using radiation boundary conditions on the outer walls of the pixel. Radiation boundaries absorb the energy incident on them. One could also use matching boundaries, also known as master-slave boundaries, to simulate periodic structures. Since the design was expected to have very low energy leakage between the pixels, both the radiation and the matching boundary conditions would give similar results. We indeed checked this for our model and found the results obtained using both the radiation and the master-slave boundaries to be comparable. We also found that the simulation with radiation boundaries converged more quickly, making it the best choice for treating the boundary conditions for our simulations.

Fig. 2 shows the schematic of our single pixel model used for HFSS simulations. The top metal cover, which is a part of the horn block, is removed (shown upside down in the figure) to show the different components inside the cavity more clearly. Although in reality the micromesh absorbers are supported by thin silicon nitride legs, we suspended the absorbers in free space to simplify the model. Because the legs are thin (1.5 µm by 4 µm) and only one of them is metalized to carry detector bias, this simplification did not affect the simulations. The absorber itself was metalized to approximately match the free space impedance to facilitate absorption. The metal backshort was realized using perfect E boundary condition on the protruded part of the backshort wafer, as shown in Fig. 2.

To determine the optical efficiency of the cavity, we needed to calculate the power absorbed by the absorber inside the integrating cavity. With HFSS, the electric and magnetic fields, current densities, and Poynting vectors can be integrated within the cavities. The power absorbed by a lossy medium can be calculated using a volume integral or a surface integral of the electric and magnetic fields [7]. Since we modeled our absorber as a
two-dimensional sheet with surface resistance $R_s$, the absorbed power can be written as

$$P_{\text{absorbed}} = \frac{1}{2R_s} \iint_S (\vec{E} \times \hat{n})^2 \, dS,$$

where $\hat{n}$ is the unit normal to the surface S. The surface resistance $R_s$ was fixed at 400 Ω / sq. for the simulations, which we previously found to be the optimum for these cavities [5], [8].

We set up our simulations with a single input port (the waveguide) and the dominant $\text{TE}_{11}$ mode excitation. For the multi-mode simulations, the waveguide port was excited with more than one mode, with the number of modes determined by the diameter of the over-moded waveguide. We carried out single pixel simulations for the P/SW, S/LW, and S/SW cavities, and also a seven pixel simulation for the P/SW cavity to predict leakage between adjacent cavities.

### B. Error Estimation and Simulation Results

In HFSS port simulations, where S-parameters are calculated at different ports of a device, one can have a fair indication of the error in simulation through a parameter in the solution setup part of the solver. In the solution setup module, there is a term “Max Delta S” which is used as a stopping criteria in the adaptive meshing steps. When the magnitude and phase of all the S-parameters change by an amount less than the specified “Max Delta S” from one iteration to the next, the adaptive meshing stops, displaying the final “Delta S” value for the simulation. This parameter “Delta S” can be used as an indicator of simulation error for port simulations. We also used conservation of energy as a check: the integrated flux flowing out through the outer walls of the pixel, plus the power absorbed in the resistive layer should add up to the incident power at the input port (usually, HFSS sets this power as 1 W). More often than not, there is some discrepancy between the calculated total power and the incident power, the extent of which depends on the coarseness of the mesh. This discrepancy in power can also be used in error estimation. For the simulation results presented here, the larger of these two error terms was taken as the calculation uncertainty.

Amongst the photometers, the most extensive simulations were carried out on the short wavelength photometer cavity (P/SW). This cavity has a 171 µm diameter circular waveguide connected to the horn, and a backshort placed at a distance of 63 µm as the nominal design parameters. The simulated performance of the cavity across the intended operating frequency range of the instrument, with the backshort positioned at the nominal quarter-wave length distance, is shown in Fig. 3. It is clear from Fig. 3 that the power absorption and the return loss performance starts declining rapidly at around 1125 GHz, with only about 37% absorption (-5 dB return loss) at 1035 GHz. However, the performance at the upper end of the band was found to be much better. To improve optical coupling efficiency at the lower edge of the band, we decided to increase the diameter of the circular waveguide by about 5%, to 180 µm. The cut-off frequency for the $\text{TM}_{01}$ mode for this guide is 1276 GHz, compared to 1343 GHz for the 171 µm diameter waveguide. The simulated performance of the P/SW cavity across the operating frequency band, with a 180 µm diameter waveguide and the backshort positioned at $\lambda_0/4$ showed substantial improvement in optical coupling efficiency across the band, specifically at the lower frequency end. At
Fig. 3. Simulated performance of the P/SW cavity across the short wavelength photometer band with a 171 µm diameter waveguide. The circles are for the absorbed power and the diamonds are for the return loss. The dotted vertical line shows the nominal band center frequency for which the different design parameters were optimized.

1035 GHz, power absorption increased to about 64% and return loss to -11 dB. Our simulations predicted only a marginal improvement in coupling efficiency with further increase of the waveguide diameter. However, by increasing the waveguide diameter further, we pay the penalty of bringing the TM\textsubscript{01} cut-off frequency even lower, right in the middle of the passband, and risk more mode conversion inside the cavity. As a result, we concluded that the P/SW design will certainly benefit from a 180 µm diameter coupling waveguide. We ran simulations to optimize the backshort position for this design and the result is shown in Fig. 4. It can be seen that the optimum backshort position is a few microns longer than the nominal $\lambda_0/4$ location. This slightly longer than a $\lambda_0/4$ backshort position can be attributed to the edge effects of the absorber where the fringe fields are created and they propagate inside the cavity with a different phase velocity.

In an attempt to investigate the possibility of using a highly over-moded waveguide for the P/SW and the S/SW cavities and study its coupling efficiency performance, we ran a few simulations with a 278 µm diameter coupling waveguide. The cut-off frequencies for this guide are 632 GHz for the TE\textsubscript{11} mode, 826 GHz for the TM\textsubscript{01} mode, 1049 GHz for the TE\textsubscript{21} mode, and 1316 GHz for the TM\textsubscript{11} and TE\textsubscript{01} modes. Since we wanted to evaluate the performance at the band center of the P/SW cavity, which is 1200 GHz, we ran simulations with the first three propagating modes, namely TE\textsubscript{11}, TM\textsubscript{01}, and TE\textsubscript{21}. First, we calculated coupling efficiencies with the waveguide input port excited with the three individual modes, excited independently one at a time, and then with all the three modes excited simultaneously. At 1200 GHz, with the input port excited with the modes one at a time, 97% of the power was absorbed for the TE\textsubscript{11} mode, 56% for the TM\textsubscript{01} mode, and 78% for the
Backshort and frontshort positions (µm)

Fig. 4. Simulated performance of the short-wavelength photometer (P/SW) cavity, with a 180 µm diameter circular waveguide, as a function of the backshort and the frontshort positions. The circles are for the absorbed power and the diamonds are for the return loss. The dotted vertical line shows the nominal backshort and frontshort position at $\lambda_0/4$.

TE$_{21}$ mode. When the port was excited with all the three modes simultaneously, the total power absorbed was only about 72%. This low power absorption can be attributed to the interaction of the modes inside the cavity. Moreover, the higher-order modes couple well to the background emission and not to the astrophysical sources since their beam patterns are not centrally peaked. Therefore, we abandoned the idea of using a over-moded waveguide and stuck with the 171 µm diameter waveguide for the feed horn coupling, and not risk the additional coupling of the higher-order modes.

It is important to pay close attention to the machining tolerances required for the frontshort metal block, to prevent crushing the detector wafer during assembly process. We ran simulations to investigate the allowable tolerance without significantly affecting the power absorption by varying the distance from the frontshort to the absorber, keeping the backshort position fixed at the optimum value as shown in Fig. 4. We did not notice any substantial change in power absorption due to the longer frontshort position from the absorber, up to about 40 µm more than the nominal $\lambda_0/4$ position. This indicates that the distance from the frontshort to the absorber is not quite as critical as the distance from the backshort to the absorber.

To investigate cross-coupling between adjacent pixels of the P/SW cavity, we simulated a seven pixel model as shown in Fig. 5. To calculate power leakage from one pixel to the other, we ran two different sets of simulations with two different input excitations. In the first case, we excited all the six pixels surrounding the central pixel with TE$_{11}$ dominant mode at 1200 GHz. The pixel at the center of the model did not have any excitation at its input port and was terminated with a matched load. Power absorbed by the central pixel absorber under such excitations was calculated and was found to be less than 0.5%. In the
second case, we only excited the pixel at the center of the array with TE_{11} dominant mode at 1200 GHz, and terminated all other ports with matched loads. Similar to the first case, power absorbed by all the other pixels in the immediate vicinity of the central pixel was found to be less than 0.5%, confirming very low cross-coupling between adjacent pixels.

For the spectrometers, we simulated both the long wavelength and the short wavelength cavities. The S/LW and the S/SW cavities were simulated with 410 µm and 190 µm diameter coupling waveguides, respectively. The simulated performance of the S/LW and S/SW cavities across the entire FTS band is shown in Fig. 6. For both the spectrometers,
the simulations were carried out with single-mode excitations, and the backshorts were optimized for the best coupling efficiency across the intended operating bands of the individual instruments. The results were found to be quite satisfactory, and we used them as a benchmark for the design goals of the instrument.

III. Fabrication, Measurements, and Results

Fabrication of silicon nitride micromesh bolometers has been described in detail by Turner et al. [9]. Here, we will elaborate on the fabrication aspects specific to the SPIRE instrument. For the detector wafer, a 1.8 µm thick film of low-stress silicon nitride was deposited using low-pressure chemical vapor deposition (CVD) on a 100 mm diameter, 300 µm thick silicon-on-insulator bonded silicon wafer. Using lift-off-photolithography technique, titanium-gold (Ti-Au) metal film was deposited to form the absorber layer, the wiring leads, and the contact layer. Using argon (Ar) reactive ion etch (RIE), the Ti-Au layer was removed selectively to expose the absorber, and CF₄ and O₂ RIE was used to selectively remove Si₃N₄ from the absorber surface. Similarly, using backside RIE processing, Si₃N₄ was removed to define the silicon frame of the detector wafer. The thermistors were developed from a polished NTD Ge wafer doped with 4.54 × 10¹⁶/cm³ concentration of gallium (Ga) and 1.29 × 10¹⁶/cm³ compensation of arsenic (Ar) [10]. The thermistor chips are about 300 µm long, 100 µm wide, and 25 µm thick. There are two 100 µm × 50 µm contact pads separated by 200 µm on the edges of the thermistors. The NTD Ge thermistors are attached at the edge of the absorber by indium (In) bump bonds with about 1–2 Newton of force using a micrometer. For the backshort wafer development, a silicon wafer was first coated with 5 nm of Ti and 500 nm of Au using lift-off-lithography. The precise backshort dimensions for different photometer and FTS bands were then etched out using deep-trench RIE.

A photograph of a prototype seven pixel short-wavelength photometer (P/SW) detector array, which was used for testing and verification of SPIRE design and simulations,
TABLE II
THEORETICAL AND MEASURED BEAM SIZES

<table>
<thead>
<tr>
<th>Array</th>
<th>Band</th>
<th>Modes</th>
<th>Calculated</th>
<th>Measured</th>
</tr>
</thead>
<tbody>
<tr>
<td>P/SW</td>
<td>250 µm</td>
<td>TE_{11}</td>
<td>7.0°</td>
<td>6.8° ± 0.2°</td>
</tr>
<tr>
<td>S/LW</td>
<td>350 µm</td>
<td>TE_{11}, TM_{01}, TE_{21}</td>
<td>5.9°</td>
<td>9.8° ± 0.1°</td>
</tr>
<tr>
<td>S/LW</td>
<td>450 µm</td>
<td>TE_{11}, TM_{01}</td>
<td>7.3°</td>
<td>8.2° ± 0.3°</td>
</tr>
</tbody>
</table>

is shown in Fig. 7(a). Fig. 7(b) shows a full-scale 43 pixel P/LW feed horn block fabricated by Custom Microwave Inc. [11]. Only two arrays, the P/SW and the S/LW, were chosen for testing as prototypes – the P/SW array was tested with a 250 µm bandpass while the S/LW array was tested with both 350 µm and 450 µm bandpasses. We decided to test the S/LW array at two different frequency bands to have a better insight on the performance by resolving the test data as a function of wavelength.

The prototype arrays were installed in a liquid helium cryostat, with a closed-cycle \(^3\)He cryocooler to cool the focal plane to the 300 mK operational temperature. The prototype array optics included a filter stack consisting of a bandpass filter, a 0.9%-transmission neutral density filter (NDF), a stack of three or four non-parallel lowpass filters, and finally a thin room temperature high density polyethylene (HDPE) dewar window. The filters were installed on the radiation shields, with indium gaskets to ensure light-tight interfaces and good thermal contact. The bolometers were configured in a balanced circuit and shared a common bias distributed through a load resistor array. The signal lines were buffered from external noise sources by low noise source-follower JFET amplifiers kept at 130 K. A shielded pre-amplifier box mounted on the outside of the dewar completed the amplifier chain.

The beams for the arrays were measured using a temperature-controlled blackbody source mounted on a two-axis linear track [12]. Each of the measured beams were fitted with a Gaussian model to determine their full width half maxima (FWHM). The case of unpolarized, fully incoherent lights were used in the Gaussian mode. The beam sizes derived from the Gaussian fits are shown in Table II, along with the expected half power beam width (HPBW) calculated from the band center frequency and feed horn aperture for the TE_{11} mode alone. The single-mode 250 µm P/SW beam size was found to be consistent with the expected TE_{11} mode diffraction limit, however, the multi-mode 350 µm and 450 µm S/LW beams were found to be larger by 68% and 15% respectively. It is clear that the S/LW beams included contributions from the TM_{01} and TE_{21} modes which were not centrally peaked.

The spectral responses of the detector and feed horn arrays were measured for each bandpass, in combination with the filter stack, using a Bruker IFS-120HR far-infrared Fourier transform spectrometer [13]. The experiment was set up to observe fringes from the spectrometer at the side exit port, with an HDPE lens to couple the beam to the focal plane. A representative measured FTS transmission spectra for each test band, along with the expected bandpass profile for each filter stack is shown in Fig. 8. The measured transmission spectra were found to be consistent with the expected centroid frequencies and widths of each bandpass, and their properties are tabulated in Table III.
The expected (upper) and the measured (lower) bandpass transmission profiles are plotted together, along with the cut-off frequency markers for each mode of the waveguides in the P/SW and S/LW arrays. The measured and the expected relative transmissions are intentionally plotted here on a different scale for clarity. The structures in the measured spectra is due to the reflection from the mylar beam splitter used in the measurement.

### TABLE III
**Bandpass Properties**

<table>
<thead>
<tr>
<th>Array</th>
<th>Band</th>
<th>( \nu ) (GHz)</th>
<th>( \Delta \nu ) (GHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P/SW</td>
<td>250 ( \mu \text{m} )</td>
<td>1212 (measured)</td>
<td>263 (measured)</td>
</tr>
<tr>
<td>S/LW</td>
<td>350 ( \mu \text{m} )</td>
<td>844</td>
<td>98</td>
</tr>
<tr>
<td>S/LW</td>
<td>450 ( \mu \text{m} )</td>
<td>657</td>
<td>124</td>
</tr>
</tbody>
</table>

The optical efficiencies of the detectors were derived from the I–V load curves measured under optical loading from blackbody sources at various temperatures which completely filled the beams [12]. Measurements were made of blackbody sources external to the dewar, as well as internal temperature-controlled “cold calibrator” blackbody source. The calculations presented here include a correction for 5% reflection off the surface of the liquid nitrogen, used as external cold load, onto room temperature surfaces. The absorbed optical power is derived by measuring the offset in electrical bias power dissipated in the detector along the lines of constant bolometer resistance. The hot and cold loads are measured in a cold–hot–hot–cold rotation so that any heating effect on the focal plane and the filters can
be detected and removed to first order by averaging the data. Optical efficiencies derived in this method from the measured load curves are listed in Table IV. The listed uncertainties on the optical efficiencies are representative of the dispersion in the measurements for three different bolometers and horns, and do not include systematic errors. The 250 µm P/SW band is mostly single-moded, and it measured an optical efficiency of 84% ± 4%, which is in good agreement with the 86% efficiency found at the center of the band in the simulations. The S/LW results are more complex due to the multi-mode nature of the bands. For the 350 µm band, an optical efficiency of 69% ± 3% was derived from measurements, assuming that the three propagating modes (two for the S/LW) are present with equal power in the bandpass. This specific cavity was not numerically simulated, but a comparison with the multi-mode simulation made for the P/SW model would provide some guidance in this regard. The multi-mode P/SW simulation yielded an optical efficiency of 72% when all three propagating modes were excited simultaneously, which agrees well with the 350 µm S/LW measurement. The 450 µm S/LW band has only two propagating modes, and it yielded a somewhat lower optical efficiency of 59% ± 3%. This indicates that the second dominant mode (TM$_{01}$) does not couple well to the detector by the horn and the cavity, which is in agreement with the observation that the 450 µm beam size show relatively less broadening from this mode than the S/SW. We also noticed from our P/SW simulations that the TM$_{01}$ mode has the lowest absorption efficiency amongst the three modes.

Our simulations predicted that the leakage between adjacent bolometer cavities is less than 0.5%. Power leakage measurements were made with the 250 µm P/SW array. All but one of the feed horn apertures were blocked in the array, and the response to a chopped external blackbody signal on all the bolometers were measured with a lock-in amplifier. For the “dark” detector adjacent to the unobstructed feed horn, leakage was measured at 0.45% of the unobstructed detector’s signal, with a signal-to-noise of 3. At the detector two pixels from the unobstructed feed horn, the leakage was found to be 0.15%, with a signal-to-noise ratio of just less than 2. This demonstrates that the leakage (crosstalk) is indeed low, consistent with our simulation results.

### IV. Conclusion

In this paper we described a new modeling technique using the HFSS three dimensional electromagnetic field solver to numerically simulate large arrays of antenna coupled integrating bolometric cavities. The simulations were detailed, and gave us access to field parameters inside the bolometer cavities to efficiently design, optimize, and predict per-
formance of large format bolometer arrays, such as the SPIRE instrument. Measurements carried out on a seven pixel prototype array allowed us to compare the simulation results with measured data, and they were found to be in close agreement. The beam sizes obtained from beam measurements and the spectral responses from FTS measurements were found to be consistent with the design theory. The optical coupling efficiency of the arrays, derived from the measured data, were found to be within a few percent of the simulated predictions, both for the single-mode and the multi-mode excitations. Low levels of cross-talk, as predicted by simulations, were corroborated by the measured low-leakage between adjacent cavities.

ACKNOWLEDGMENTS

We thank Jonas Zmuidzinas of Caltech, Imran Mehdi and Peter Siegel of JPL for their support and encouragements. We also thank Anthony Murphy of National University of Ireland for useful discussions about feed horns, and Jacob Kooi of Caltech for his helpful suggestions on HFSS simulations.

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